

NUMBERS

N (NATURAL NUMBERS)	=	Normal counting numbers 1,2,3,...
W (WHOLE NUMBERS)	=	N + Zero
I (INTEGERS)	=	W + Negative Numbers
Q (RATIONAL NUMBERS)	=	I + Fractions
R (REAL NUMBERS)	=	Q + Irrational Numbers
C (COMPLEX NUMBERS)	=	R + Imaginary Numbers

To check if a number **N** is prime, one can check if **N** is divisible by any prime less than or equal to \sqrt{N} .

The order of priority for basic mathematical operations is **VBODMAS**, where:

V (Vinculum or Bar)	}	These need to be solved before anything else
B (Bracket)		
O (Of)	-	Indicates a multiplication of higher priority
D (Division)	}	If only multiplication and division remain, we go from left to right
M (Multiplication)		
A (Addition)	}	If only addition and subtraction remain, we go from left to right
S (Subtraction)		

(A good mnemonic to remember this order is "Very Bored Of Doing Mathematics At School")

In terms of a number line, we can define the following functions for a real number x

[x]: Greatest integer less than or equal to x = the first number to the left of x on the number line. Also known as rounded-down value.

L(x): Least integer greater than or equal to x = the first number to the right of x on the number line. Also known as rounded-up value.

| x |: Absolute value of x = the distance from 0 to x on the number line. Also, known as modulus.

Note that:

$[x] \leq x \leq L(x)$ (equal only if x is an integer)

$|x| \leq x$ (equal only when x is a non-negative)

PROBLEMS:

1. State True / False / Cannot be determined

a) Even + Odd + odd = Even **b)** Even * Odd * Even * Odd = Even **c)** (Even + Odd) * (Even + Odd) = Even

d) Positive + Positive + Negative = Positive **e)** Positive * Positive * Negative * Negative = Positive

f) (Positive * Positive) + (Negative * Negative) - Negative = Positive

g) All fractions can be written as mixed fractions

h) All recurring numbers can be written in a rational format.

2. Insert $>$, $=$ or $<$ signs in between the following pairs of fractions:

a) $11/14$ $13/16$ b) $11/8$ $13/10$ c) $14/19$ $7/9$ d) $3/14$ $5/23$

e) $217/229$ $219/231$ f) $271/263$ $461/473$

3. Show that for any number N, it is true that $N \times N! = (N+1)! - N!$

4. Match the following expressions with their appropriate values:

S.No.	Expression	Option	Value
1.	$\sqrt{80.88} + 7 \div 4.1 - (-0.9) - (2.99)^2$	a	1.0
2.	$117 \div (31 + 4 \times 2) \div 2$	b	3.0
3.	$0.25 \times \overline{1.99 + 1.99} + 16.39 \div 8.19$	c	1.4
4.	$7.17 - \sqrt{35.78} + 1 + 0.8$	d	1.8
5.	$(2.1699 + 3.8298) \times (0.465 - 0.161)$	e	1.5

5. Let $n! = 1 \times 2 \times 3 \times 4 \times \dots \times n$ for integer $n \geq 1$. What could be the value of $1! + (2 \times 2!) + (3 \times 3!) + (4 \times 4!) + \dots + (10 \times 10!)$?

a) $11 \times 11!$ b) $11!$ c) $11! - 1$ d) $11! + 1$

6. The number of people writing a test is a prime number less than 200. The ratio of the people pass to those who fail, could be:

a) $82 : 83$ b) $75 : 78$ c) $76 : 81$ d) $91 : 78$

7. The post office has stamps of Rs. 1, Rs. 3 and Rs. 7. Which of the following totals cannot be achieved by buying exactly 100 stamps?

a) Rs. 298 b) Rs. 600 c) Rs. 473 d) Rs. 440

8. Let p, q and r be distinct integers, that are odd and positive. Which of the following must be true?

a) $(p+q)(q+r)(r+p)$ is negative b) $(p+q)(q+r)(r+p)$ is even
 c) $(q-p)(q-r)(p-r)$ is positive d) $(p+q)(q+r)(r+p)$ is odd

9. Which of the following statements is true?

a) $[x] - L(x) = -1$ b) $[x] + |x| \geq 0$ c) $|x+y| > |x-y|$ d) $L(x) + |x| \geq 0$

10) The product of 10 integers is 1. Can their sum is equal to 0?

11) Can you find 5 odd numbers which add up to 100?

12) Find out all the Prime numbers between 1 and 100 and memorise them.